



**SIGGRAPH 2021**

**UNBIASED EMISSION AND  
SCATTERING IMPORTANCE SAMPLING  
FOR HETEROGENEOUS VOLUMES**

**WEI-FENG WAYNE HUANG  
PETER KUTZ,  
YINING KARL LI  
MATT JEN-YUAN CHIANG**



Hello Siggraph 2021 and thank you for having us.

Please refrain from  
screen grabs or recording.



THANK YOU!

Please refrain from recording these talks. This helps us so we can continue to share our work with you.

The logo for Walt Disney Animation Studios, featuring the classic script 'Walt Disney' followed by 'ANIMATION STUDIOS' in a sans-serif font, with a small Mickey Mouse head icon to the right.

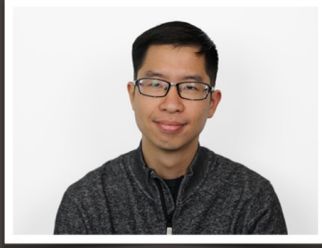
# Unbiased Emission and Scattering Importance Sampling for Heterogeneous Volumes

WEI-FENG WAYNE HUANG  
PETER KUTZ  
YINING KARL LI  
MATT JEN-YUAN CHIANG

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Today I would like to discuss some recent development works we did to improve the volumetric emission and scattering sampling for our in house rendering system, Hyperion.





**Wei-Feng Wayne Huang**  
SENIOR SOFTWARE ENGINEER  
*RENDERING*

I am Wayne Huang from Walt Disney Animation Studio, and I will present the work for our team

# New System, New Challenges

**Spectral and Decomposition Tracking for Rendering Heterogeneous Volumes**

PETER KUTZ, Walt Disney Animation Studios  
RALF HABEL, Walt Disney Animation Studios  
YINING KARL LI, Walt Disney Animation Studios  
JAN NOVAK, Disney Research

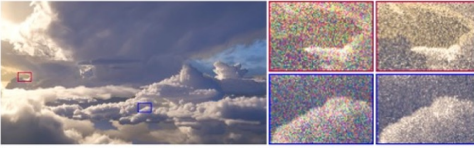


Figure 1. A landscape rendered with a combination of our spectral and decomposition tracking techniques, which gracefully handle chromatic media and reduce collision coefficient evaluations. The insets on the right were computed in equal time, with our method yielding 3.5x lower MSE than delta tracking.

We present two novel unbiased techniques for sampling free paths in heterogeneous participating media. Our *decomposition tracking* accelerates free path construction by splitting the medium into a control component and a residual component and sampling each of them separately. To minimize expensive evaluations of spatially varying collision coefficients, we define the control component to allow constructing free paths in closed form. The residual heterogeneous component is then homogenized by adding a fictitious medium and handled using weighted delta tracking, which removes the need for computing strict bounds of the extinction function. Our second contribution, *spectral tracking*, enables efficient light transport simulation in chromatic media. We modify free-path distributions to minimize the fluctuation of path throughput and thereby reduce the estimation variance. To demonstrate the correctness of our algorithms, we derive them directly from the radiative transfer equation by extending the integral formulation of null-collision algorithms recently developed in reactor physics. The mathematical framework, which we thoroughly review, encompasses existing trackers and postulates an entire family of new estimators for solving transport problems; our algorithms are examples of such. We analyze the proposed methods in canonical settings and on production scenes and compare to the current state of the art in simulating light transport in heterogeneous participating media.

CCS Concepts • **Computing methodologies** → **Rendering**; **Key tracing**

Additional Key Words and Phrases: participating media, volume rendering, free-path sampling, transmittance, delta tracking, ratio tracking, color

ACM Reference format:  
Peter Kutz, Ralf Habel, Yining Karl Li, and Jan Novak. 2017. Spectral and Decomposition Tracking for Rendering Heterogeneous Volumes. *ACM Trans. Graph.* 36, 4, Article 111 (July 2017), 14 pages.  
DOI: <http://dx.doi.org/10.1145/3072993.3073665>

1 INTRODUCTION  
Accurate and efficient simulation of radiative transfer in participating media is essential in many domains, such as nuclear reactor design, medical imaging, scientific visualization, and realistic image synthesis. The animation and visual effects industry, in particular, employs rich and complex volumetric structures (such as smoke, fire, or clouds) and translucent materials (such as marble, wax, or skin)

At Walt Disney Animation Studios we recently revamped our in house volume rendering system. This new system allows us to render white clouds among other things in an unbiased way and we described our methods in this paper published in SIGGRAPH 2017.

However, when it was deployed, we found that some scenarios are challenging to the new system. So, today I am going to talk about some further improvements that we made along the way to overcome these challenges.

# Overview

## Introduction

- Volume rendering background
- Null-collision formulation
- Challenges

## Emission sampling improvements

## Scattering sampling improvements

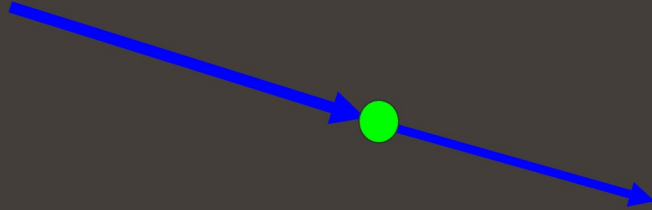
I would like to first briefly introduce the null-collision formulation of volume rendering, which is what our system based on. And then I'll dive deeper into our improvements on emission and scattering sampling.

# Volume Rendering Background

Let's first talk about some background for volume rendering

# Volume Rendering Recap

Absorption  $\mu_a$  : how much radiance is absorbed passing through medium

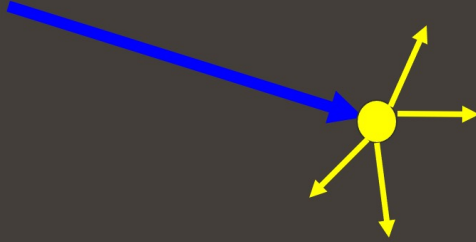


Volume rendering is composed of the following medium interactions:  
Absorption - how much energy is absorbed passing through the medium.

# Volume Rendering Recap

Out-scattering  $\mu_s$  : how much radiance is scattered out passing through the medium

Extinction  $\mu_t = \mu_s + \mu_a$

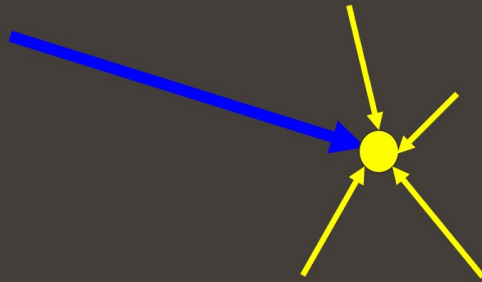


Out-scattering, how much energy being scattered to other directions by the medium.

The combination of the absorption and out-scattering is commonly referred to as extinction, which accounts for the net energy loss when a ray traveling in a volume.

# Volume Rendering Recap

In-Scattering  $\mu_s$  : how much radiance is scattered in passing through the medium

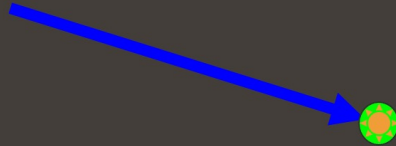


In-scattering, how much energy being scattered into the current directions by the medium.



# Volume Rendering Recap

Emission  $L_e$  : how much radiance is emitted from the medium after absorption

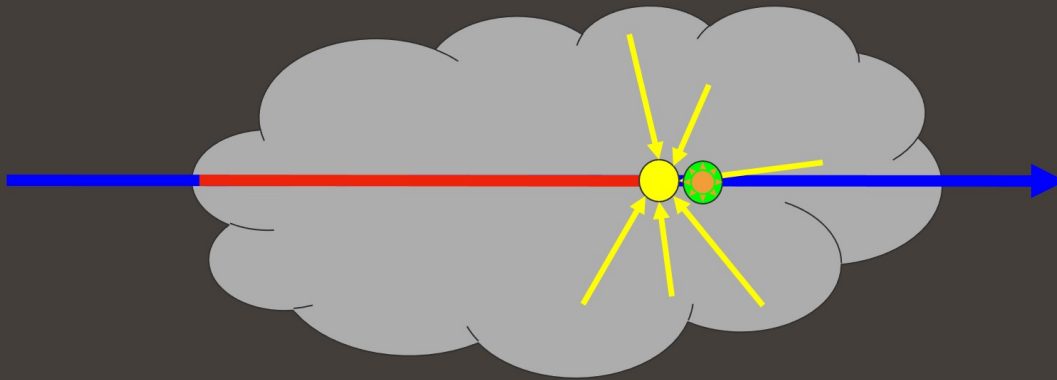


Also there is emission, describing the amount of energy emitted from a medium after absorption.

In-scattering and emission together accounts for the net energy gain when traveling through a volume.

## Volume Rendering Equation (VRE)

$$L(\mathbf{x}, \omega) = \int_0^{\infty} T(\mathbf{x}, \mathbf{y}) [\mu_s(\mathbf{y}) L_s(\mathbf{y}, \omega) + \mu_a(\mathbf{y}) L_e(\mathbf{y}, \omega)] d\mathbf{y}$$

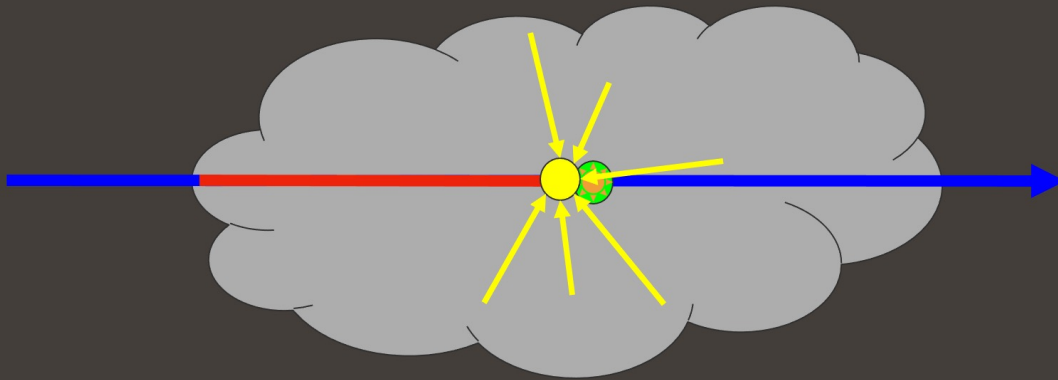


Putting them together we got the volume rendering equation:

To solve for the equation, for each points along the ray segment, we need to gather the emission term and the source term inside the volume and attenuate it with the transmittance term.

# Volume Rendering Equation (VRE)

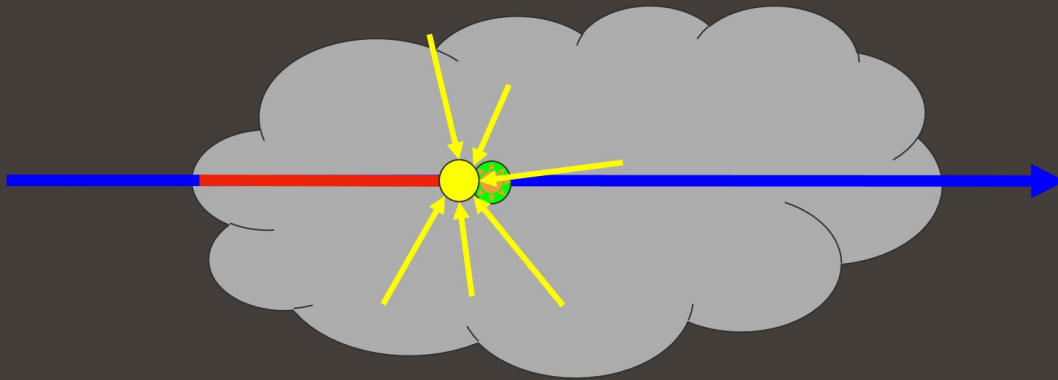
$$L(\mathbf{x}, \omega) = \int_0^{\infty} T(\mathbf{x}, \mathbf{y}) [\mu_s(\mathbf{y}) L_s(\mathbf{y}, \omega) + \mu_a(\mathbf{y}) L_e(\mathbf{y}, \omega)] d\mathbf{y}$$



We then integrate it along the entire segment.

# Volume Rendering Equation (VRE)

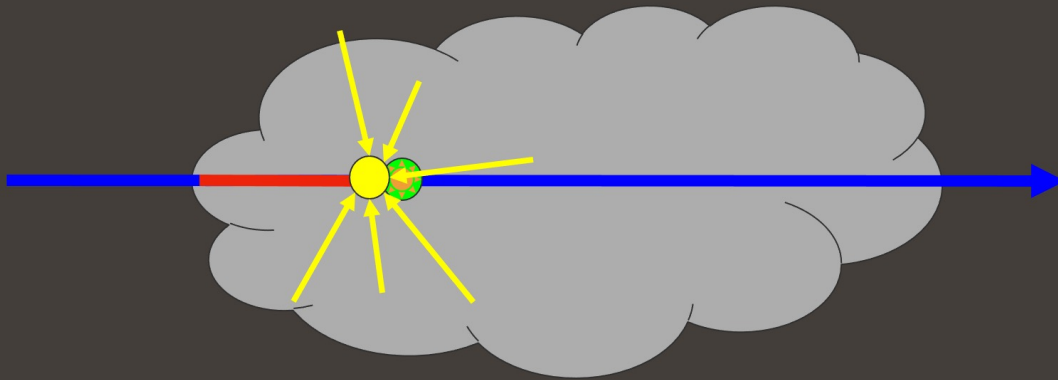
$$L(\mathbf{x}, \omega) = \int_0^{\infty} T(\mathbf{x}, \mathbf{y}) [\mu_s(\mathbf{y}) L_s(\mathbf{y}, \omega) + \mu_a(\mathbf{y}) L_e(\mathbf{y}, \omega)] d\mathbf{y}$$



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## Volume Rendering Equation (VRE)

$$L(\mathbf{x}, \omega) = \int_0^{\infty} T(\mathbf{x}, \mathbf{y}) [\mu_s(\mathbf{y}) L_s(\mathbf{y}, \omega) + \mu_a(\mathbf{y}) L_e(\mathbf{y}, \omega)] d\mathbf{y}$$



We then integrate it along the entire segment.

# Volume Rendering Equation (VRE)

$$L(\mathbf{x}, \omega) = \int_0^\infty T(\mathbf{x}, \mathbf{y}) [\mu_s(\mathbf{y}) L_s(\mathbf{y}, \omega) + \mu_a(\mathbf{y}) L_e(\mathbf{y}, \omega)] d\mathbf{y}$$

$$T(\mathbf{x}, \mathbf{y}) = e^{-\int_0^y \mu_t(\mathbf{x}-s\omega) ds}$$

Can't be analytically solved

$$L_s(\mathbf{x}, \omega) = \int_{S^2} f_p(\omega, \bar{\omega}) L_i(\mathbf{x}, \bar{\omega}) d\bar{\omega}$$

This triggers recursions

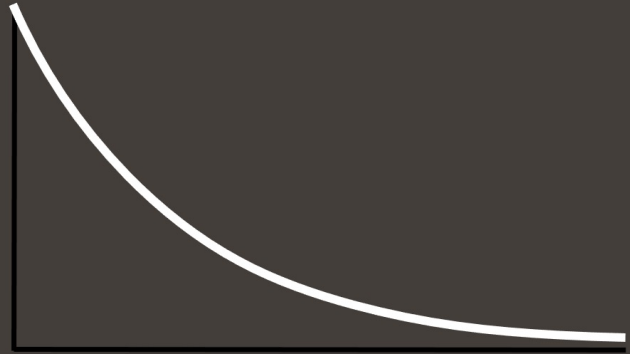
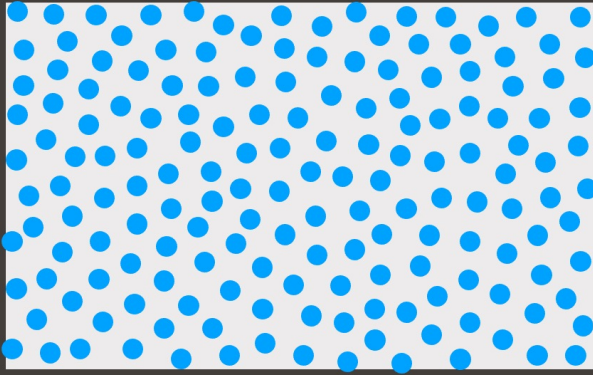
The reason the volume rendering equation is difficult to solve is because

Evaluating the source terms requires recursively launching new rays, so a highly scattering volume often takes thousands of bounces for a path to leave the volume.

On top of that evaluating the transmittance term requires another integration which often can't be analytically solved.

# Transmittance Homogeneous

● = scattering

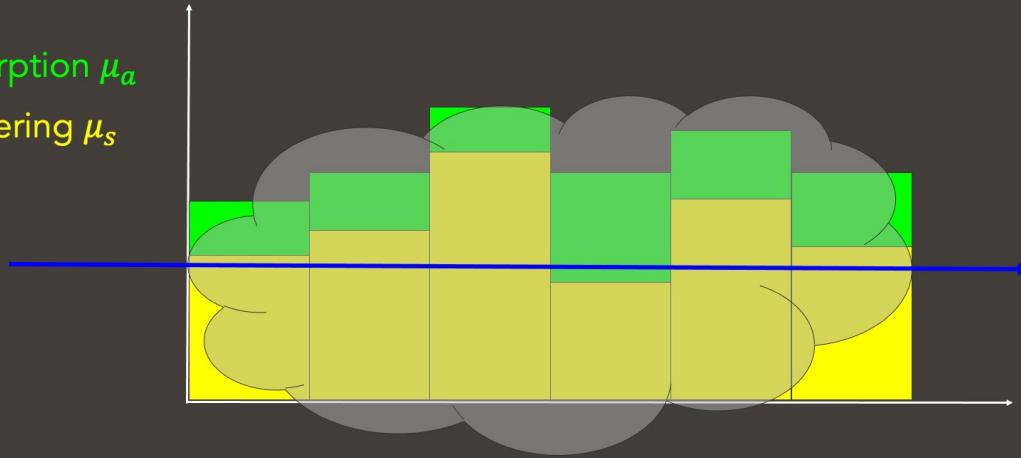


Homogeneous volume is an exception. It has constant extinction coefficient throughout, so that the transmittance integral can be analytically computed.



# Transmittance Heterogeneous

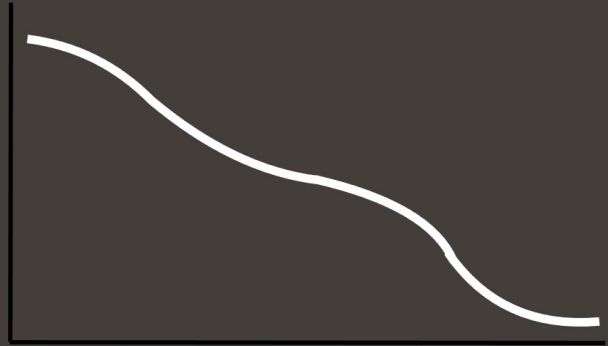
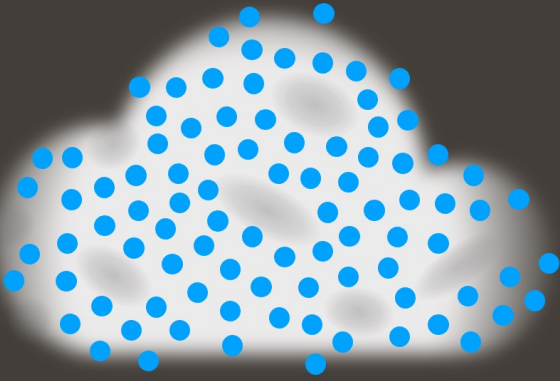
- Absorption  $\mu_a$
- Scattering  $\mu_s$



However, most of the interesting volumes in film production are heterogeneous.

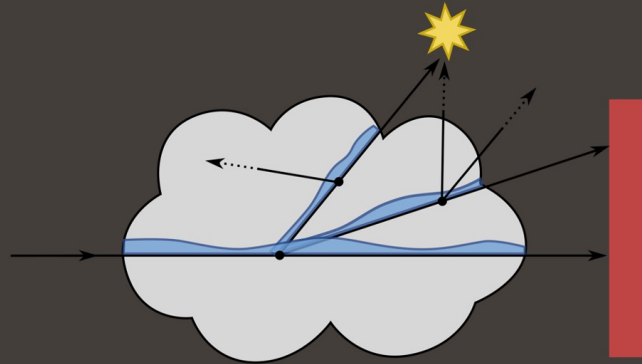
# Transmittance Heterogeneous

● = scattering



And the transmittance in this case relies on numerical approximations or Monte Carlo estimations.

## Old System



One popular technique in production volume rendering solves the equation by ray marching through volume along each ray segment to numerically approximate the transmittance. A detailed importance table is built for each ray segment to sample a location for the next emission or scattering event.

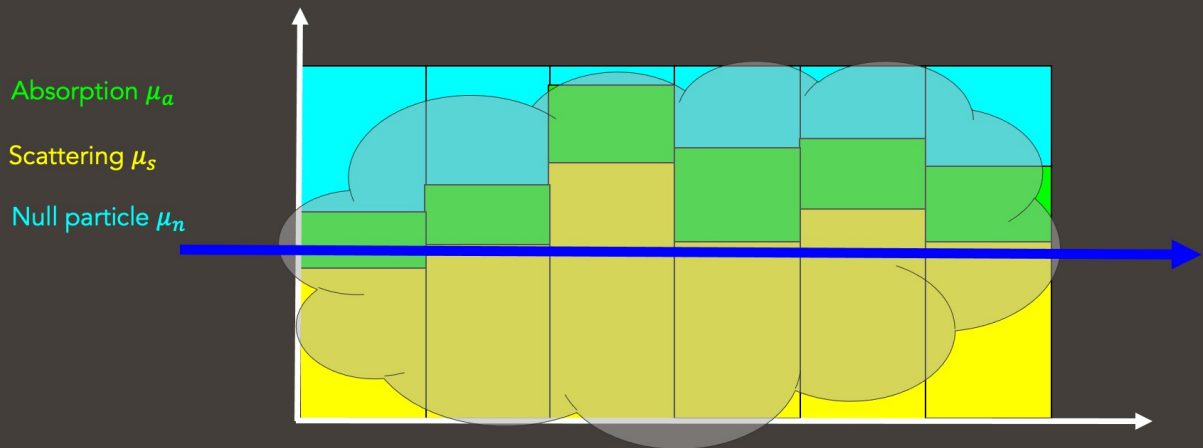
This technique works well for low-scattering volumes but its high computational cost for each sample prevents us from rendering thick volumes like a cloud.

# Null-Collision Formulation

This limitation motivated us to adopt a Null-Collision based approach.

# Null-Collision Formulation

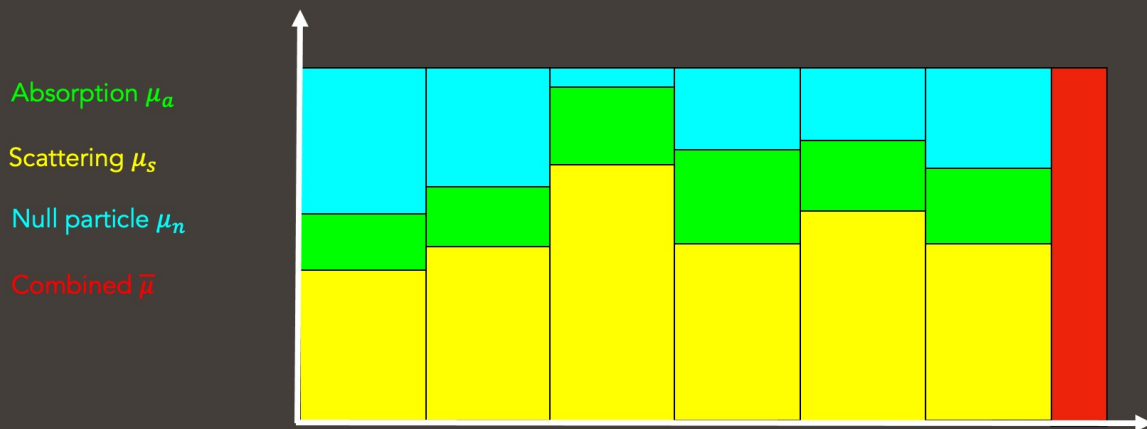
We can fill in null particles to homogenize the volume



The basic idea of null collision theory or a so called tracking based system is to homogenize the volume by filling it with “null” particles that don’t invoke any volume interaction.

# Null-Collision Formulation

And use combination of three coefficients to integrate the volume




And in this “homogenized” volume, the combined extinction coefficient is then constant, so that we can sample transmittance analytically.

## VRE: Null Collision Edition

The volume rendering equation can be rewritten using the null-collision formulation:

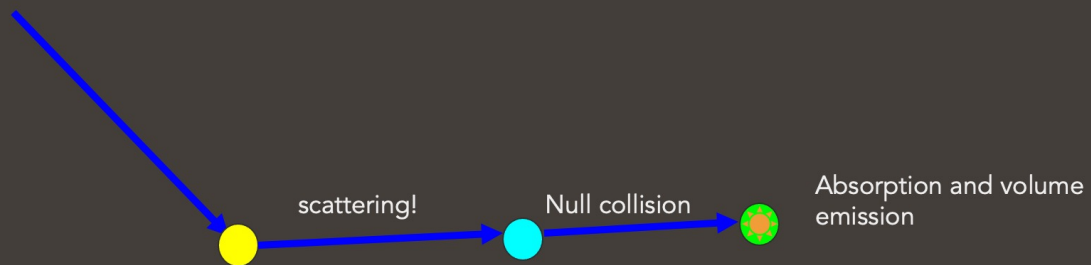
$$L(\mathbf{x}, \omega) = \int_0^\infty T(\mathbf{x}, \mathbf{y}) [\mu_s(\mathbf{y})L_s(\mathbf{y}, \omega) + \mu_a(\mathbf{y})L_e(\mathbf{y}, \omega)] dy$$


$$L(\mathbf{x}, \omega) = \int_0^\infty \bar{T}(\mathbf{x}, \mathbf{y}) [\mu_s(\mathbf{y})L_s(\mathbf{y}, \omega) + \mu_a(\mathbf{y})L_e(\mathbf{y}, \omega) + \mu_n(\mathbf{y})L(\mathbf{y}, \omega)] dy$$

We can rewrite the volume rendering equation taking all these into account. Pay attention to the updated and now analytic transmittance term and the additional null-collision term.



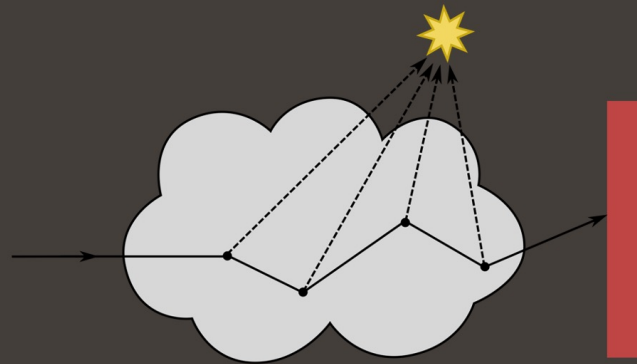
## Rendering with Null Collision VRE



Evaluating the Null-Collision Formulation of Volume Rendering Equation becomes a random walk process.

We first start with sampling a free path distance using the combined extinction coefficient, and then probabilistically pick an event out of the absorption, scattering and null-collision events.

# New System



Compared to the ray marching solution, such random walk tracking system no longer requires front to back importance table construction for each scattering event. With each sample having a much lower cost,

# Multiple Scattering



Hyperion

photo by Kevin Udy  
[coclouds.com/436](http://coclouds.com/436)

It makes multiple scattering in volumes practical. And we were able to reproduce results indistinguishable from photographs.

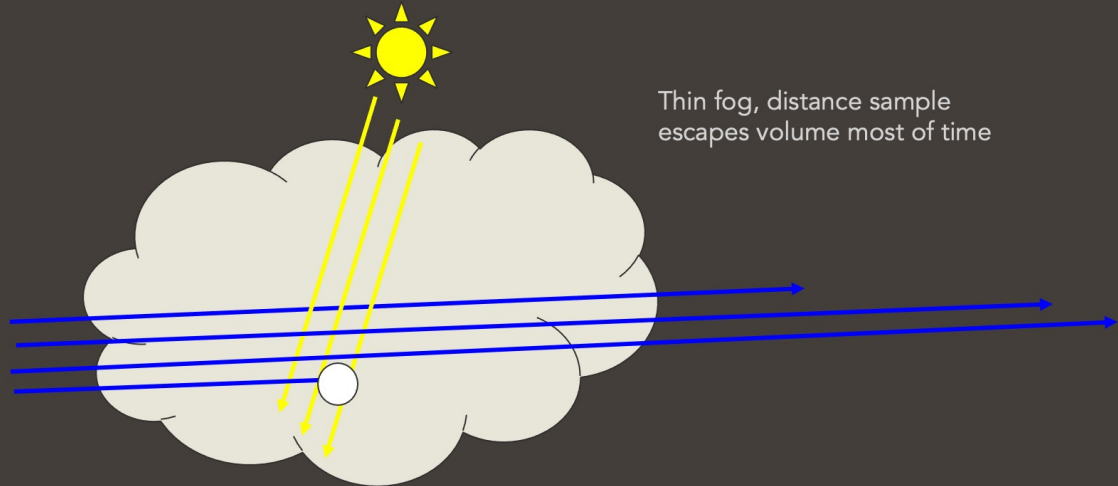


We were also able to render full cloudscales with unbounded path lengths...

# Challenges

However, as I mentioned in the very beginning of the talk, we learned from the production of *Ralph Breaks the Internet* and *Frozen 2*, that such volume system also had its disadvantages.

# Thin Volume



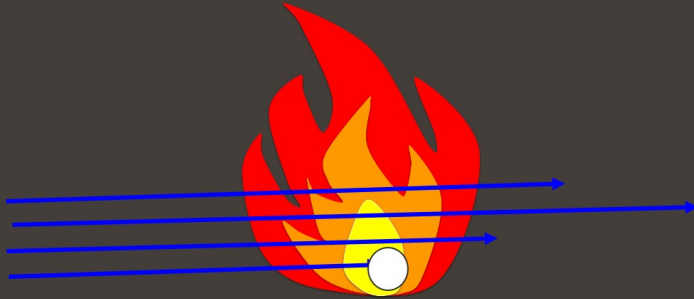
For example, when rendering thin fog, the average sampled distance is quite large. As most of the rays go right through the volume, there are few chances to sample a scattering event to evaluate the illumination.

## Thin Volume



As a result, effects such as god ray or light shaft were often noisy.

# Fire



Same issue applies to fire as well. As fire usually has low extinction, the random walk process again takes too big of a step, passing through fire easily.

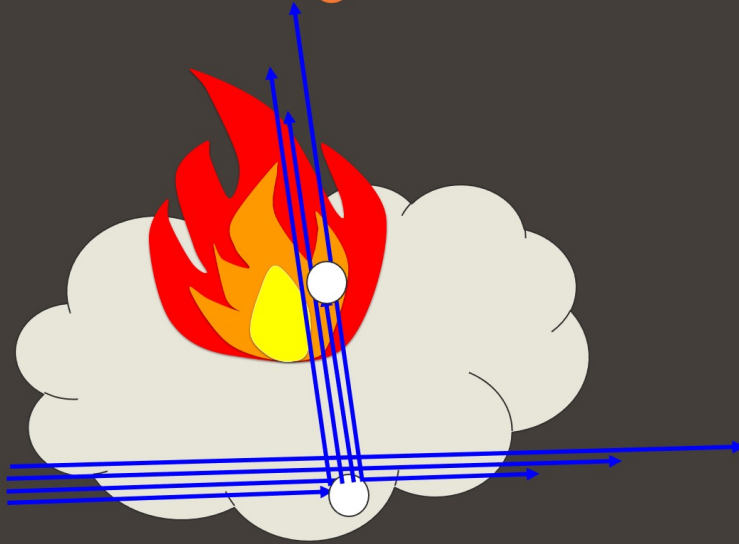


# Fire



So, capturing details in flame is quite challenging.

## Fire illuminating thin volume



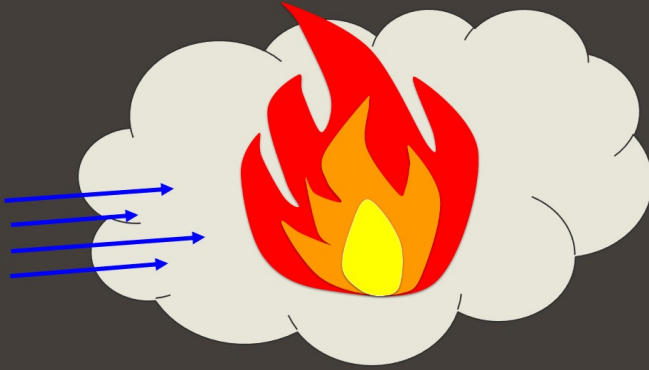
And not too surprisingly, illuminating a thin volume with fire makes render efficiency even worse.

## Fire illuminating thin volume



Here is a production example of such case, and it often resulted in noisy renders.

## Fire behind thick volume



Moreover, on the opposite case, where we have fire inside a thick volume, it is equally challenging since the average sampled distance in this case is now too short that a ray rarely makes to the fire.

## Fire behind thick volume



This is problematic not just for rendering an explosion, but also when such explosion illuminates the environment.

# Raya Visual Development



Fast forward to the pre-production of the film *Raya and the Last Dragon*.  
From the early visual development work, we saw there were god rays,  
light shafts,

# Raya Visual Development



A misty tunnel lit by torches,



# Raya Visual Development



A city full of torch lights covered in thin fog,



# Raya Visual Development



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And even characters made of emissive volumes wrapped in dense smoke...

It became apparent that some improvements to the existing volume system would have to be made in order to render the film.

# Emission Sampling

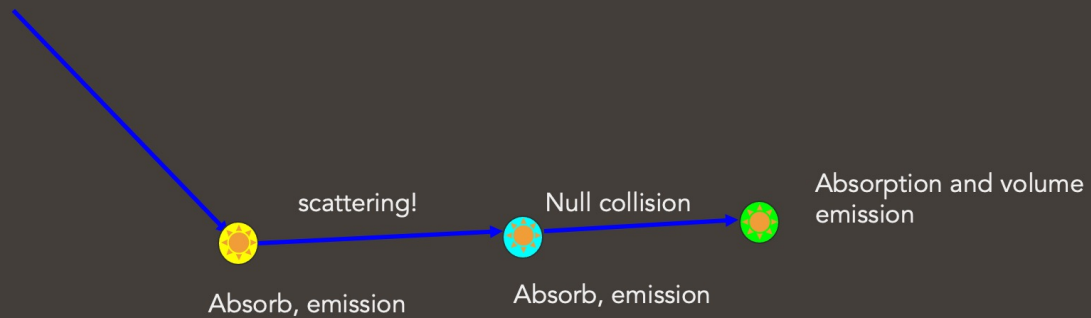
We first take a look at what we improved on the emission sampling side:

## Decouple Emission from Absorption Event



We noticed that the emission term was only evaluated when absorption events happen. This is an intuitive interpretation of the random walk since we can associate each interaction to one particular event.

## Decouple Emission from Absorption Event



However, we realized that we can actually always evaluate absorption and emission in all three types of events and still be mathematically correct. We don't want to evaluate scattering and null collision events together since it would cause rays to split into two different directions, but absorption won't split the ray and therefore we can always evaluate it. This increased evaluation frequency is compensated for by the increased probability, which makes the estimator converge to the same result faster.

## Decouple Emission

Gathering emission at:  
absorption only



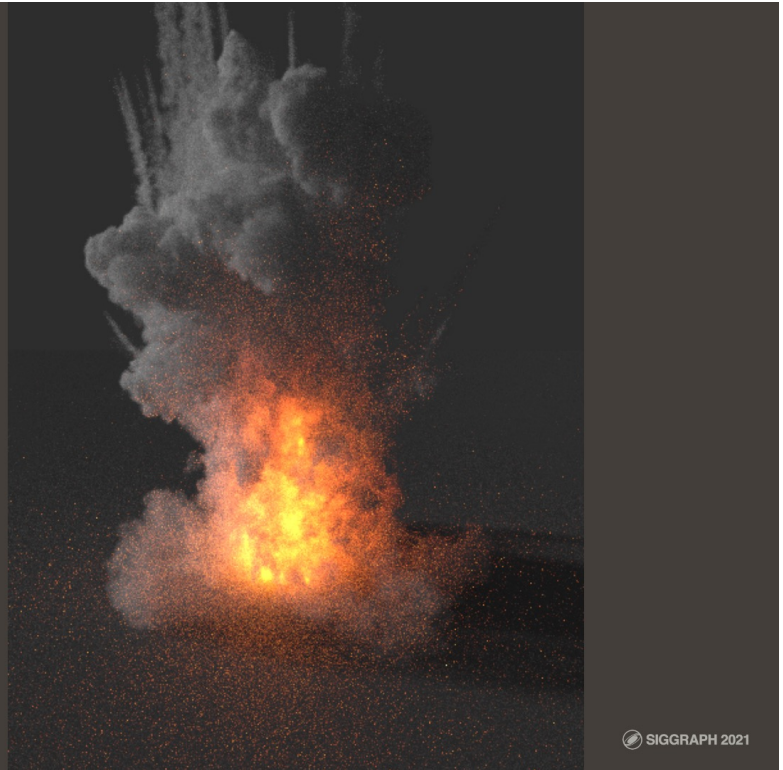
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This is a test render where the renderer only evaluates emission according to probability  $P_a$

## Decouple Emission

Gathering emission at:  
all steps



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And this is an equal sample test render that evaluates emission on all types of events. The noise reduction is quite noticeable.

## Dedicated Transmittance Estimator

A variation of the null collision tracking estimator: set  $P_n$  to 1 and deterministically evaluate null-collision events. This is called ratio tracking [\[Novak14\]](#) for transmittance estimation:

$$L(\mathbf{x}, \omega) = \int_0^d \overline{T}(\mathbf{x}, \mathbf{y})$$

$$(\mu_a(\mathbf{y})L_e(\mathbf{y}, \omega) + \mu_s(\mathbf{y})L_s(\mathbf{y}, \omega) + \mu_n(\mathbf{y})L(\mathbf{y}, \omega))dt$$

Ratio tracking is a dedicated null-collision formulation transmittance estimator that works by ignoring the emission and scattering terms from the equation and allowing the null-collision event to be carried out at all time...

## Dedicated Emission Estimator

Since emission can be evaluated with all types of events, we can extend ratio tracking to gather emission contribution along the ray:

$$L(\mathbf{x}, \omega) = \int_0^d \overline{T}(\mathbf{x}, \mathbf{y})$$

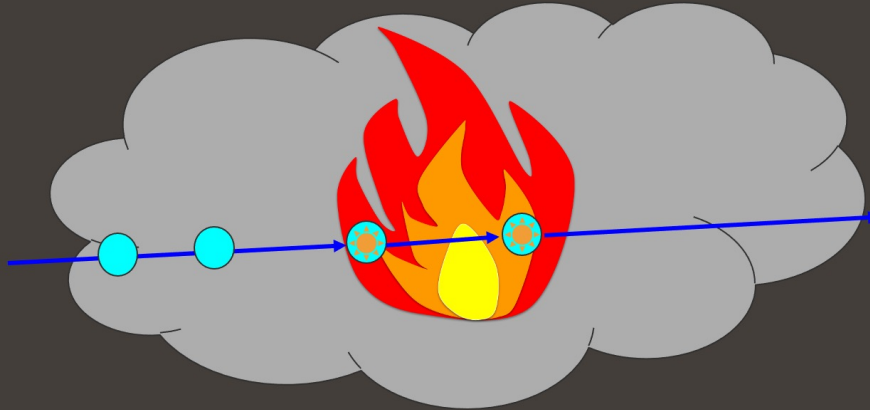
$$(\mu_a(\mathbf{y})L_e(\mathbf{y}, \omega) + \mu_s(\mathbf{y})L_s(\mathbf{y}, \omega) + \mu_n(\mathbf{y})L(\mathbf{y}, \omega))dt$$

As we discussed earlier, emission can be evaluated along with other volume interaction events. If we split the scattering and emission integration into two estimators, we can extend ratio tracking to gather emission contributions along the ray.



## Emission Ratio Tracking

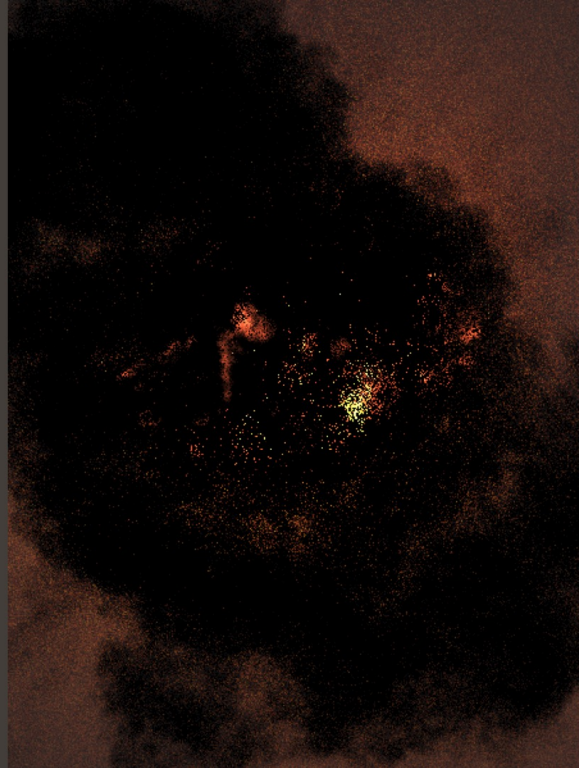
We can further force  $P_n$  to 1 and gather all emission events along the ray so that the ray can go through dense smoke to reach the emissive region:



We call this extension “emission ratio tracking”. By setting the null collision probability to 1, this emission tracker can go through dense volumes to reach the emissive region without being absorbed or scattered too early.

# Emission Ratio Tracking

Force  $P_n$  to 1: NO



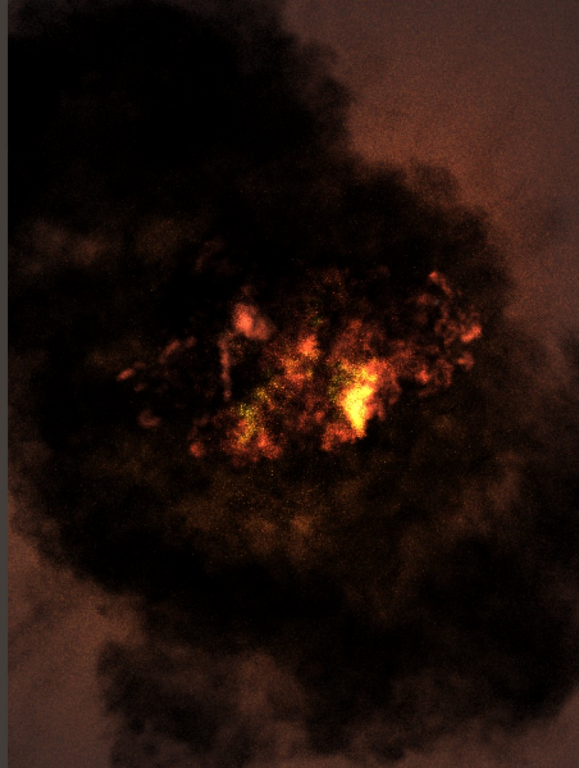
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This is a test render that evaluates emission on all types of events. The emission term is difficult to gather since a lot of samples get scattered or absorbed by dense smoke before reaching the emissive region.

# Emission Ratio Tracking

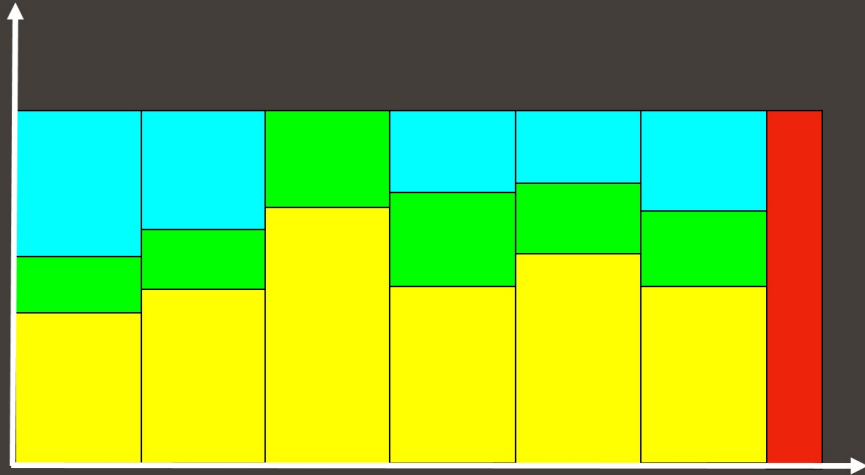
Force  $P_n$  to 1: YES



And this is an equal sample test render using emission ratio tracking. The ray now can go through the entire volume and gather the emission term that is buried in the heavy smoke.

# Majorant Boost

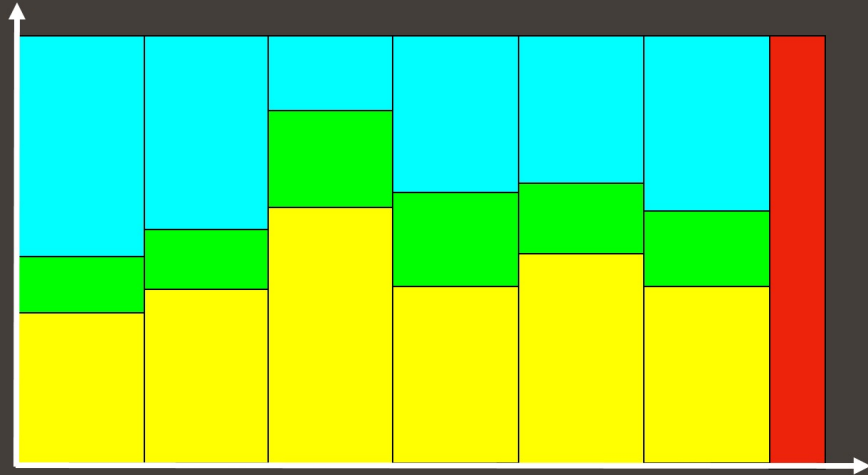
Conventionally,  $\bar{\mu}$  is the local maximum  $\mu_a$  and  $\mu_s$



For null-collision tracking performance reasons,  $\mu_{\text{bar}}$  is usually based on a local maximum of the absorption and scattering coefficients

# Majorant Boost

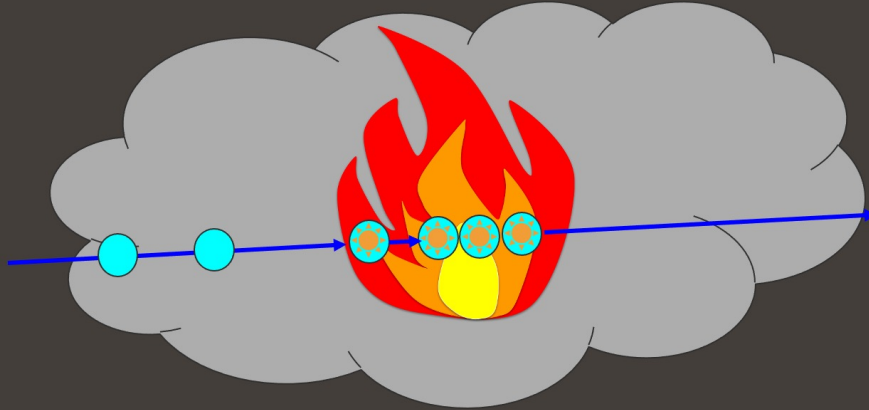
But you can actually fill in arbitrarily more null-collision particle  $\mu_n$ . Updated  $\bar{T}, \bar{\mu}$  will compensate the integration result



But the null-collision formulation puts no limitations on the amount of null-collision particles  $\mu_n$  to homogenize the volume.

## Majorant Boost

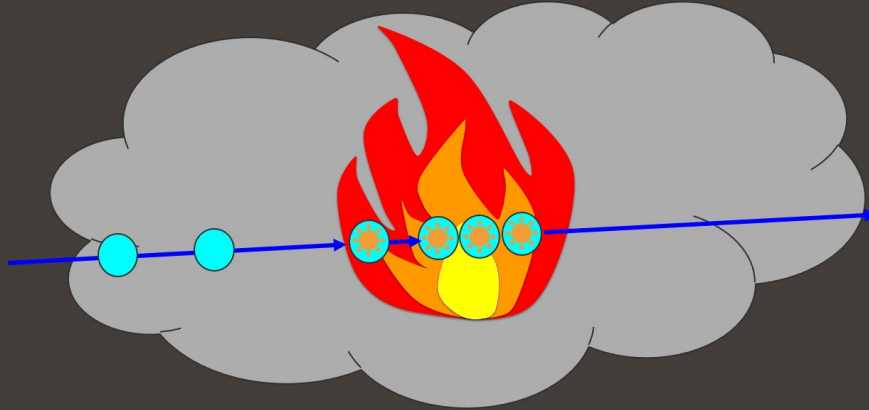
To gather more samples along the emission, we can use local  $\max(\mu_t, \mu_a L_e)$  instead of local  $\max(\mu_t)$  as  $\bar{\mu}$



Since a higher number of  $\mu_{\text{bar}}$  will result in smaller tracking steps, instead of just using the local maximum of  $\mu_t$  as  $\mu_{\text{bar}}$ , we use the local maximum of  $\mu_t$  “AND”  $\mu_a$  by  $L_e$  as  $\mu_{\text{bar}}$ , so we can take more steps in highly emissive regions.

## Majorant Boost

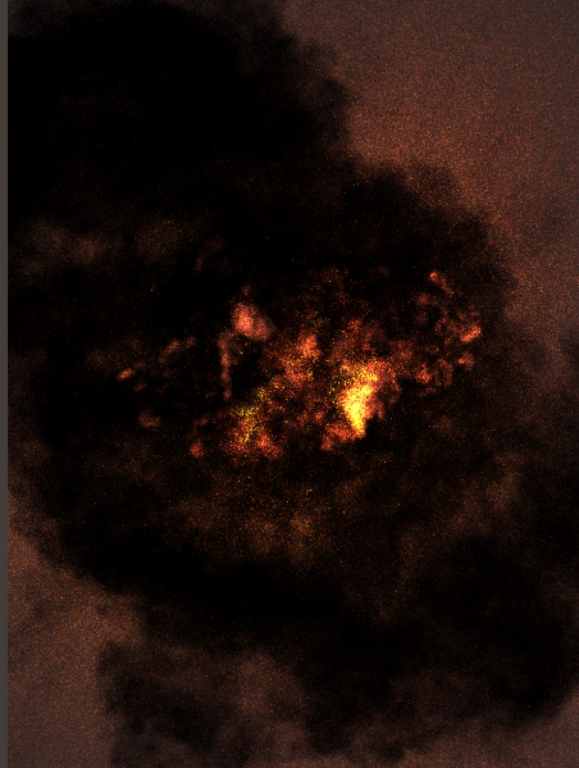
Note that we still clamp  $\bar{\mu}$  under voxel size so that distance samples won't get so short that we step in the same voxel many times (2x speed up in some scenes)



We learned from production experience that  $\mu_{\text{bar}}$  also needs to be clamped under the volume grid voxel size to prevent stepping through the same voxel too many times. We think that finding a more principled way to determine the optimal  $\mu_{\text{bar}}$  value is a good topic for future research.

# Majorant Boost

Free-path-sampling coefficient:  
max extinction

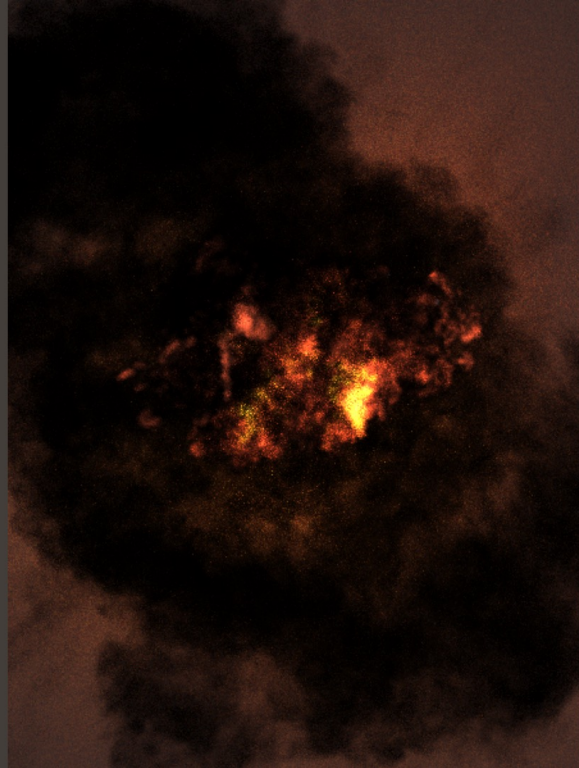


This is a test render using emission ratio tracking and using the  $\mu_t$  local maximum as  $\mu_{\bar{}}$



# Majorant Boost

Free-path-sampling coefficient:  
max extinction and emission



And this is a test render also using emission ratio tracking, but using the local maximum of  $\mu_t$  AND  $\mu_a$  by  $L_e$  as  $\mu_{\bar{}}$

## Emissive Volume as Light Source



With these techniques, we can now efficiently render emissive volumes that are directly visible to camera, but we would also like to illuminate the scene with these emissive volumes.

# Next Event Estimation

Requires three function definitions:

```
Color EmissiveVolume::eval(const Vec3& shadingPoint, const Vec3& wi)
```

```
Color EmissiveVolume::sampleDirection(const Vec3& shadingPoint, Vec3& wi)
```

```
Float EmissiveVolume::pdf(const Vec3& shadingPoint, const Vec3& wi)
```

In path tracing, this is typically done by Next Event Estimation. For next event estimation, we already know how to evaluate the emissive volume in a given direction, but we still need some way to sample the emissive volume like a light source and some way to evaluate its PDF along a direction.

# Next Event Estimation

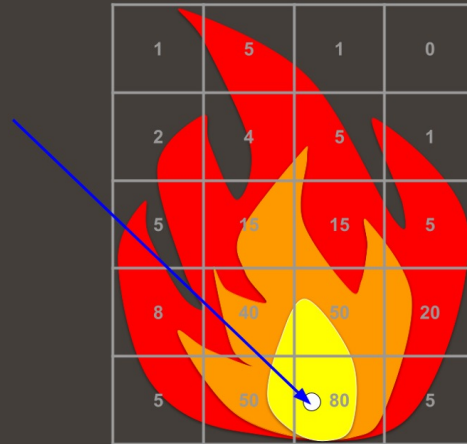
Similar to [Villemin13](#), we use 3D energy distribution grid to drive light samples:



We extended Villemin's solution for emissive volume next event estimation. We use a coarse grid representing the 3D energy distribution to make sure that hotter regions have a higher chance of receiving light samples.

# Next Event Estimation

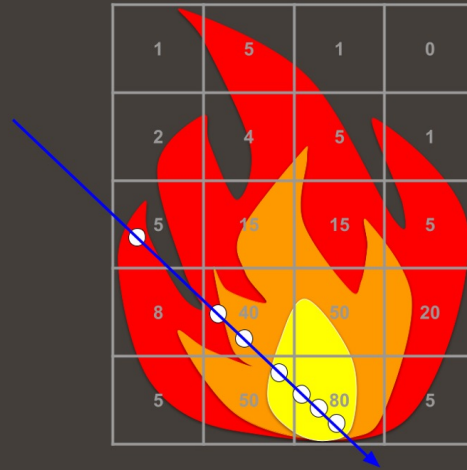
But instead of just evaluating the sampled point...



Villemin's technique used point sampling, which has difficulty when emission is obscured by heavy smoke or when the emissive region is large. These cases require very high sample counts to capture emission details in glossy reflections.

# Next Event Estimation

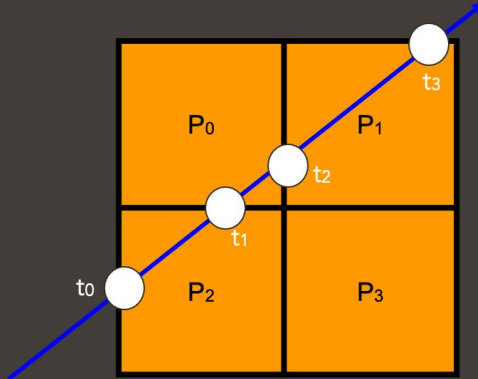
...we use above emission ratio tracker to evaluate the entire line:



Therefore, we use the emission ratio tracker introduced earlier to evaluate every tracking point along the ray, gathering more information in each light sample.

# MIS Pdf

To MIS with bsdf samples, the pdfs stored in the 3d distribution grid nodes that our ray passes through need to be summed up and converted to the solid angle domain [Simon18]



$$p_{\sigma}(\omega) = \int_0^{\infty} p_x(t)t^2 dt$$
$$= P_0(t_1^3 - t_0^3)/3 + P_1(t_2^3 - t_1^3)/3 + P_0(t_3^3 - t_2^3)/3$$

Finally, to use multiple importance sampling to combine bsdf samples with light samples in the solid angle domain, we need to integrate pdfs stored in distribution grid cells that the light sample ray passed through using a Jacobian transform.

# Pseudocode for Eval/Pdf

This gives us a self contained emission sampler similar to other light types for NEE:

---

## Algorithm 1

---

```
1: function EVALUATEEMISSION( $x, \omega, d$ )
2:    $w \leftarrow 1, L_e \leftarrow 0$ 
3:   repeat
4:      $\Delta t \leftarrow -\frac{\ln(1-\zeta)}{\mu}$ 
5:      $x \leftarrow x - \Delta t \times \omega$ 
6:      $L_e \leftarrow L_e + w \times \frac{\mu_a(x) \times L_e(x)}{\mu}$ 
7:      $w \leftarrow w \times \frac{\mu_n(x)}{\mu}$ 
8:   until  $(t \leftarrow t + \Delta t) > d$ 
9:   return  $L_e$ 
10: end function
```

---

---

## Algorithm 2

---

```
1: function PDFEMISSION( $x, \omega$ )
2:    $p = 0$ 
3:   for voxel  $v$  along ray( $x, \omega$ ) do
4:      $[t_0, t_1] \leftarrow v$  entry/exit
5:      $p \leftarrow p + \frac{(t_1^3 - t_0^3)}{3} \times \text{pdf}(v)$ 
6:   end for
7:   return  $p$ 
8: end function
```

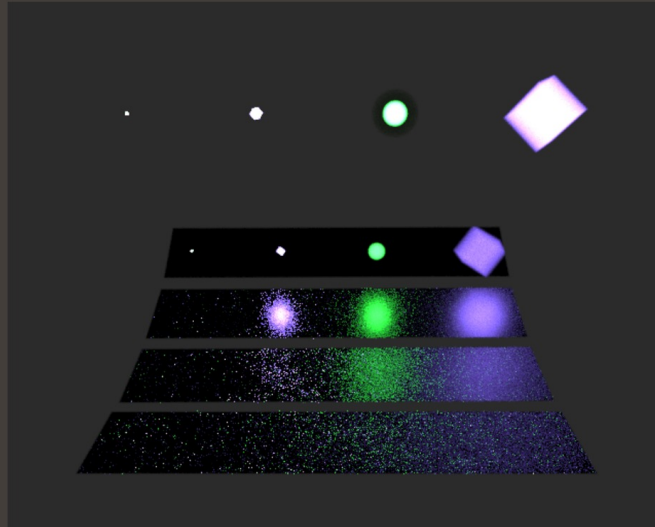
---

This gives us a self-contained emission sampler like any other type of light source. The pseudo code can also be found in the talk abstract.



## Before Next Event Estimation

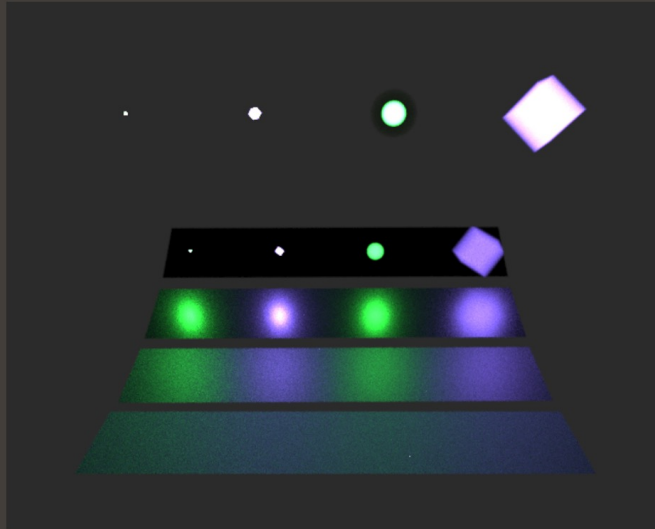
Without  
directional  
sampling



This is a test render using only bsdf samples to capture the emissive volume contribution; the diffuse and high roughness surfaces are noisy since few samples are lucky enough to hit the emissive volume.

# After Next Event Estimation

With  
directional  
sampling



And this is an equal sample test render combining next event estimation with bsdf sampling using multiple importance sampling.



We put the above emission sampling improvements together in our volume renderer. In this before and after equal-sample-count comparison from production, our emission sampling improvements capture noticeably more detail in the surface/volume illumination.

# Scattering Sampling

Now we switch gears to look into the scattering sampling side of the problem.

## Factors Involved in Scattering Integration

$$L(\mathbf{x}, \omega) = \int_0^\infty T(\mathbf{x}, \mathbf{y}) [\mu_s(\mathbf{y}) L_s(\mathbf{y}, \omega) + \mu_a(\mathbf{y}) L_e(\mathbf{y}, \omega)] d\mathbf{y}$$

$$T(\mathbf{x}, \mathbf{y}) = e^{-\int_0^y \mu_t(\mathbf{x}-s\omega) ds}$$

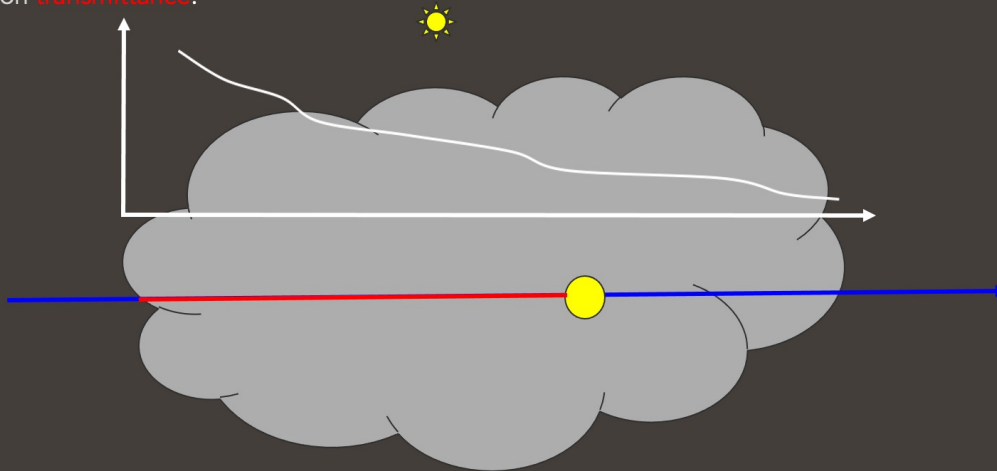
$$L_s(\mathbf{x}, \omega) = \int_{S^2} f_p(\omega, \bar{\omega}) L_i(\mathbf{x}, \bar{\omega}) d\bar{\omega}$$

Volume scattering is mainly affected by the following factors in the volume rendering equation:

Transmittance, Radiance and Phase function

# Transmittance

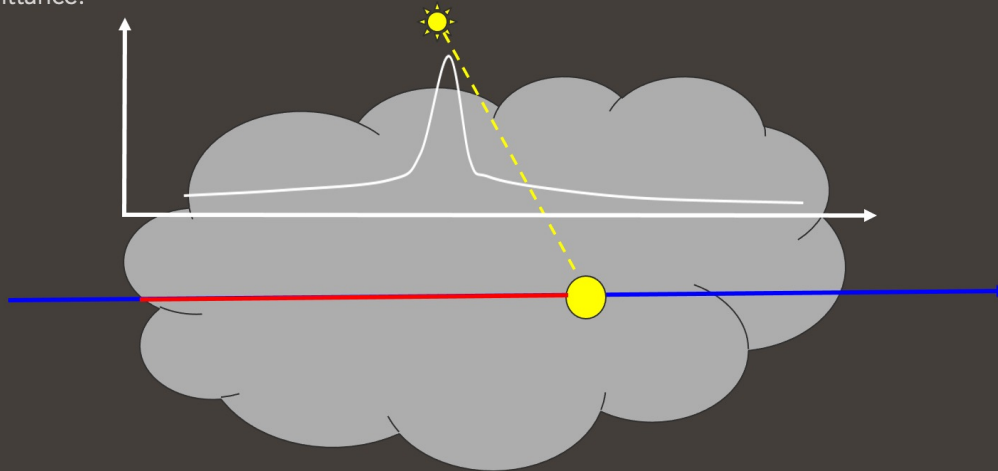
Null-Collision Tracking gives us scattering samples distributed based on **transmittance**:



Null-collision distance sampling gives us scattering samples based on the transmittance term

# Radiance

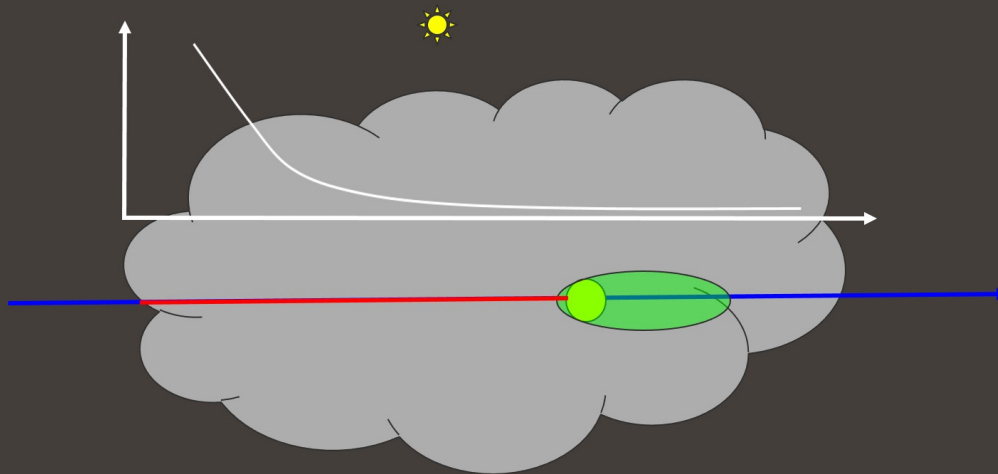
The **radiance** distribution can be quite different from transmittance:



The radiance term distribution can be quite different from the transmittance, and there are techniques like equi-angular sampling for cases dominated by this term...

# Phase Function

An anisotropic phase function also has its own shape:



A forward scattering phase function will have a front peak distribution.

Common solution to handle these different distributions is to use multiple importance sampling to combine different sample strategies



## Recent Research Breakthrough:

We can't come up the pdf of an arbitrary scattering point in null-collision tracking for MIS purpose until [Miller19]'s recent research breakthrough:

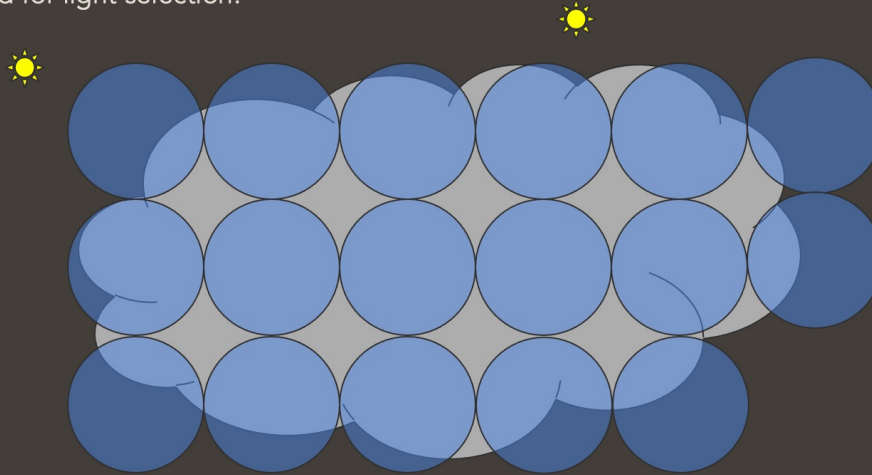
### A null-scattering path integral formulation of Light Transport

- Miller et al. SIGGRAPH 2019

However, compute distance sampling pdf for an arbitrary scattering point for MIS was an unsolved problem until the recent research breakthrough. After Miller et al. derived the analytical pdf for null-collision path formulations, we started experimenting with combining other strategies with null collision tracking.

# Cache Points

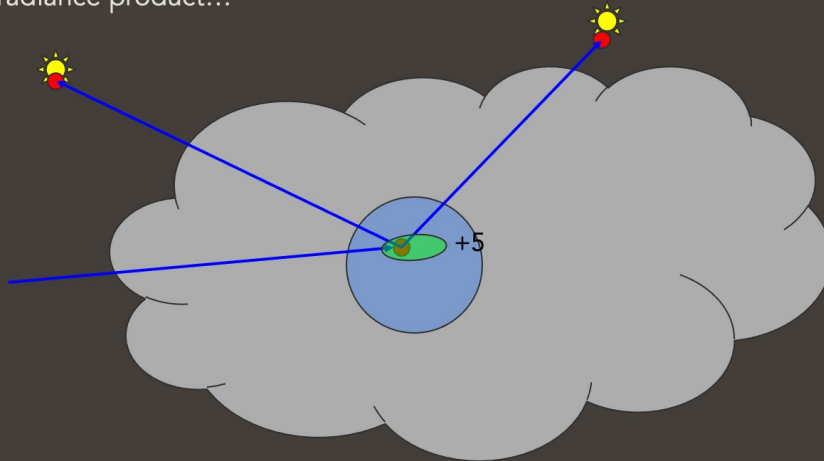
Probe spheres data structure that was developed for light selection:



Hyperion uses a probe-spheres data structure called cache points to handle many-light selection, and we thought it is possible to reuse them to guide volumetric scattering distance samples.

# Scattering Sample Weight

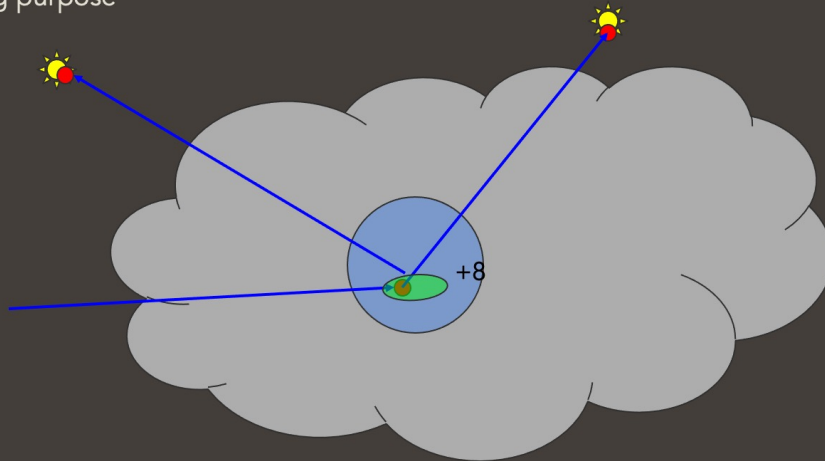
We precompute a score value based on phase/radiance product...



For each probe sphere populated in volume, we go through emissive sources and draw samples from the emissive sources, from the scattering point within the probe sphere, and from the camera lens in order to approximate the scattering source term. We use this approximation to assign a score value, which we call the scattering sample weight.

# Scattering Sample Weight

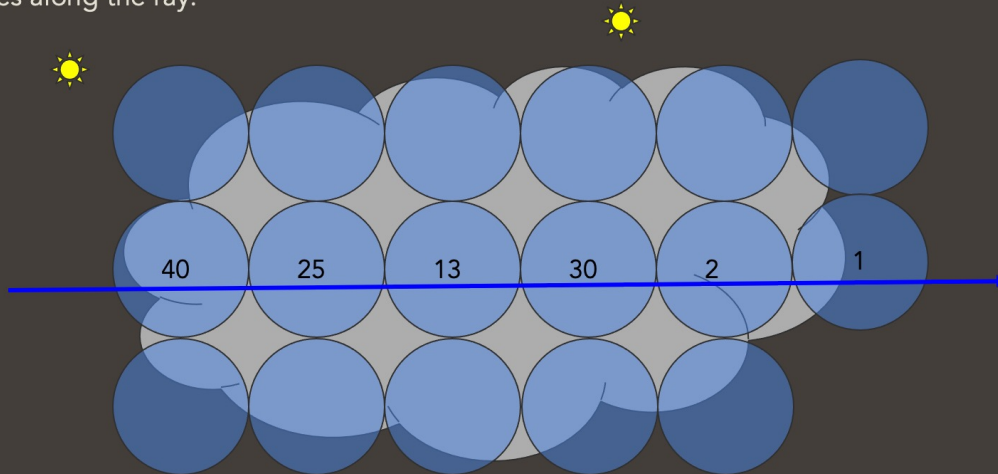
...and store in probe sphere for rendering time guiding purpose



We then store the score value into the probe sphere for later guiding purpose

# Probe Spheres Distribution

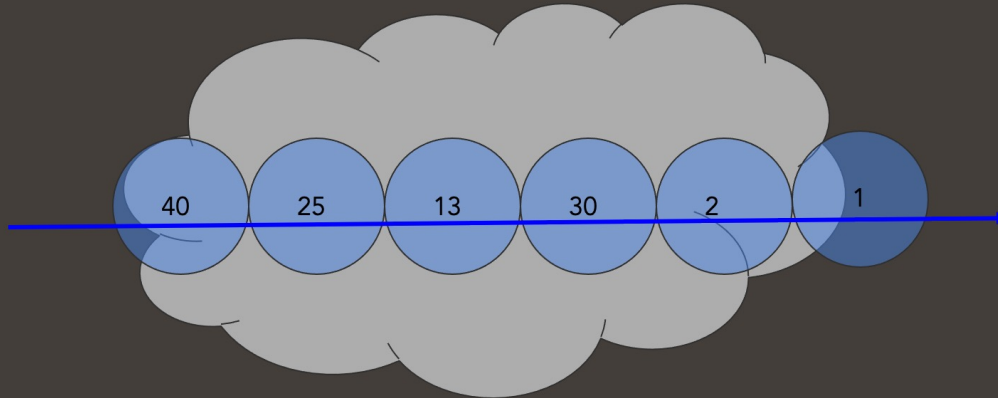
In render time we query the nearby probe spheres along the ray:



During the ray tracing stage, we query the nearby probe spheres along the ray.

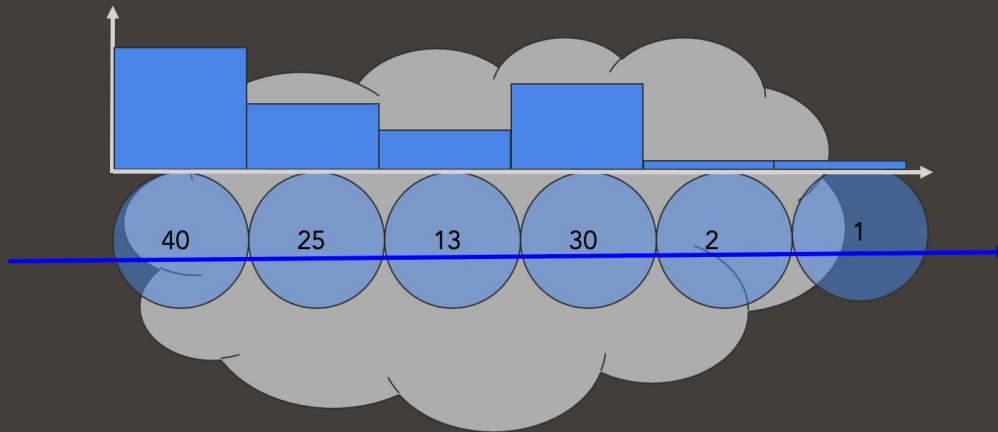
# Probe Spheres Distribution

In render time we query the nearby probe spheres along the ray:



# Probe Spheres Distribution

Generate a 1D piecewise distribution to sample scattering points

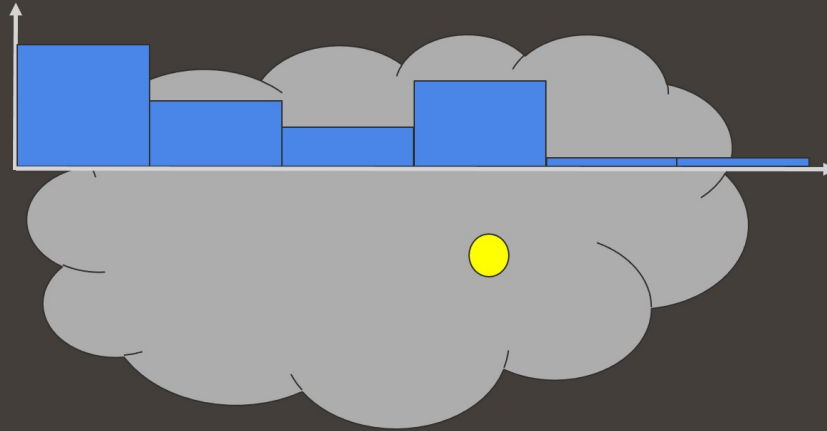


then use these score values to form a 1D distribution to draw scattering samples. this sampling strategy is only used to generate scattering points for primary-ray direct lighting now to keep the overhead down.

## Form a path using probe spheres

Pick up scatter point through 1D distribution first:

$$p_{probes}(\bar{x}) = p_{select}(x_k)$$



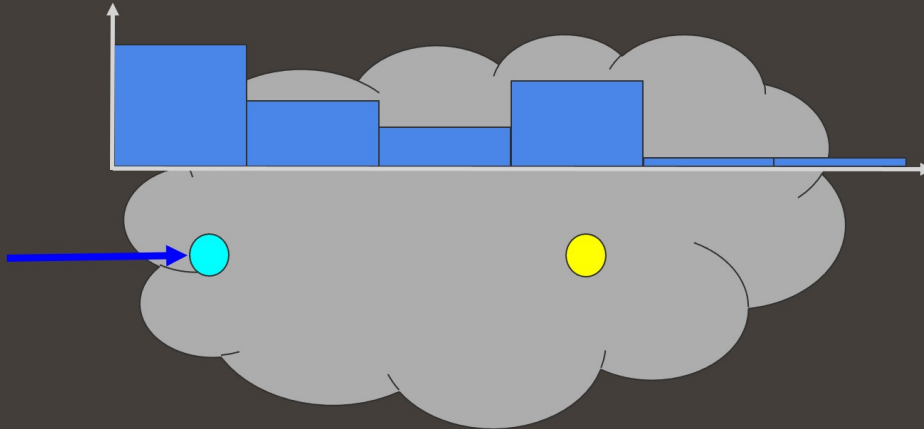
To form the full path that contains the null-collision path vertices for MIS purpose, we use the 1D distribution first to pick up the scattering point



## Form a path using probe spheres

Then use ratio tracking to fill up the entire path

$$p_{probes}(\bar{x}) = p_{select}(x_k) \bar{T}(x_0, x_1) \bar{u}(x_1)$$

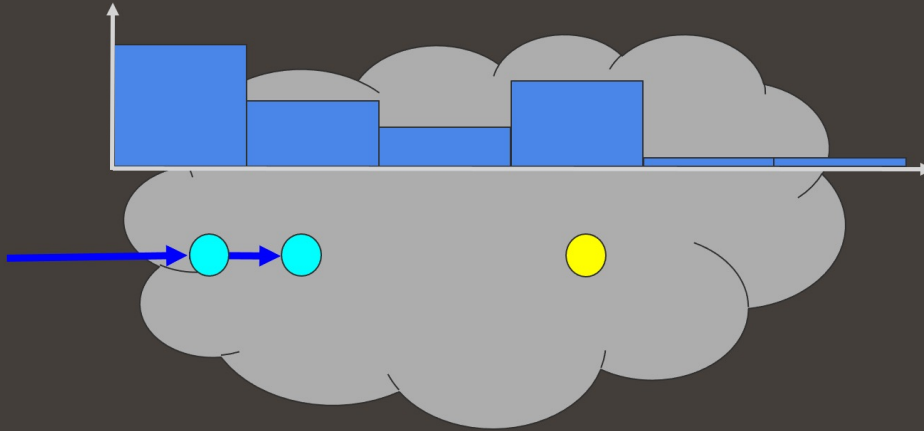


We then use ratio tracking moving towards the scattering point, and update the path pdf

## Form a path using probe spheres

Then use ratio tracking to fill up the entire path

$$p_{probes}(\bar{x}) = p_{select}(x_k) \bar{T}(x_0, x_1) \bar{u}(x_1) \bar{T}(x_1, x_2) \bar{u}(x_2)$$

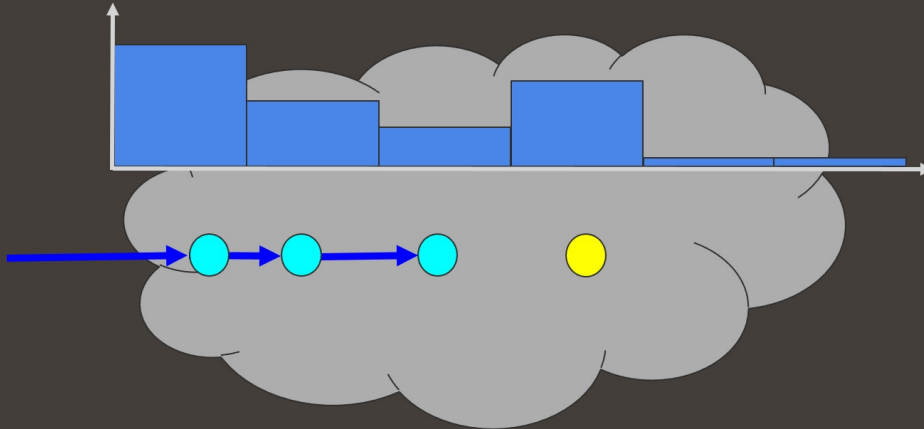


repeat the distance sampling process...

## Form a path using probe spheres

Then use ratio tracking to fill up the entire path

$$p_{\text{probes}}(\bar{x}) = p_{\text{select}}(x_k) \bar{T}(x_0, x_1) \bar{u}(x_1) \bar{T}(x_1, x_2) \bar{u}(x_2) \bar{T}(x_2, x_3) \bar{u}(x_3)$$

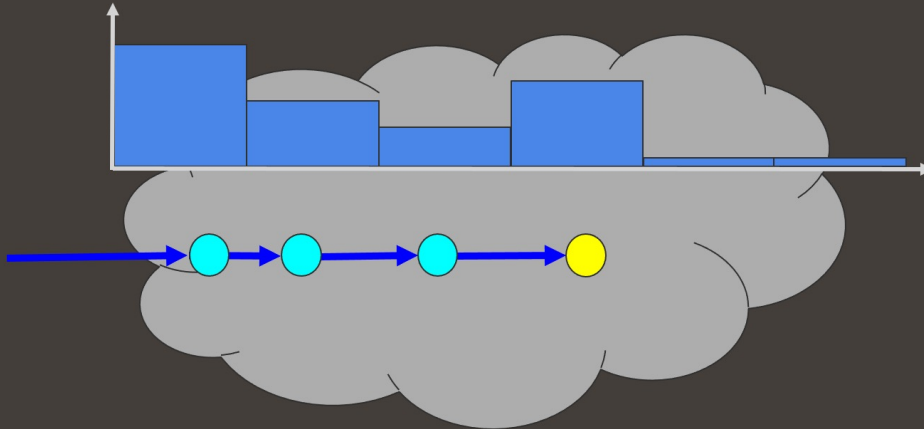


...and update the corresponding pdf...

## Form a path using probe spheres

Then use ratio tracking to fill up the entire path

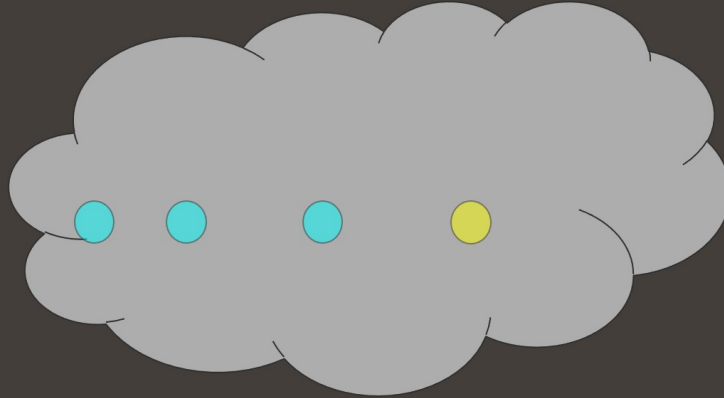
$$p_{probes}(\bar{x}) = p_{select}(x_k) \bar{T}(x_0, x_1) \bar{u}(x_1) \bar{T}(x_1, x_2) \bar{u}(x_2) \bar{T}(x_2, x_3) \bar{u}(x_3) \bar{T}(x_3, x_k)$$



...until distance sampling passes through the scattering point

## Form a path using Null-Collision Tracking

Incremental distance sampling with  $P_n, P_s$  test:

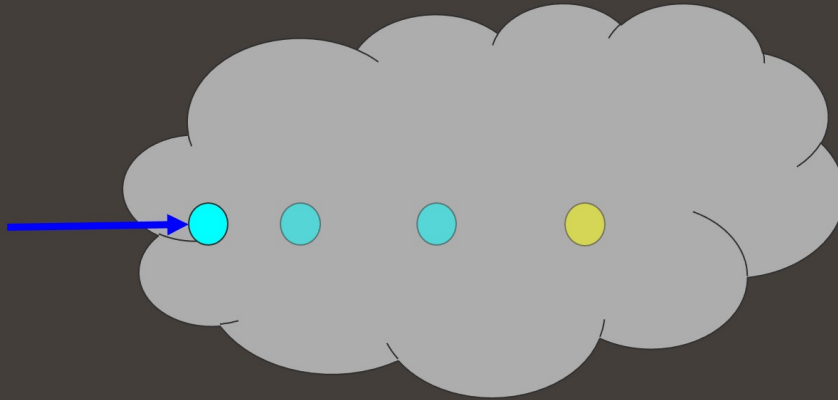


To formulate the same path using null-collision tracking to get the pdf...

## Form a path using Null-Collision Tracking

Incremental distance sampling with  $P_n, P_s$  test:

$$p_{null}(\bar{x}) = \bar{T}(x_0, x_1) \bar{\mu}(x_1) P_n(x_1)$$

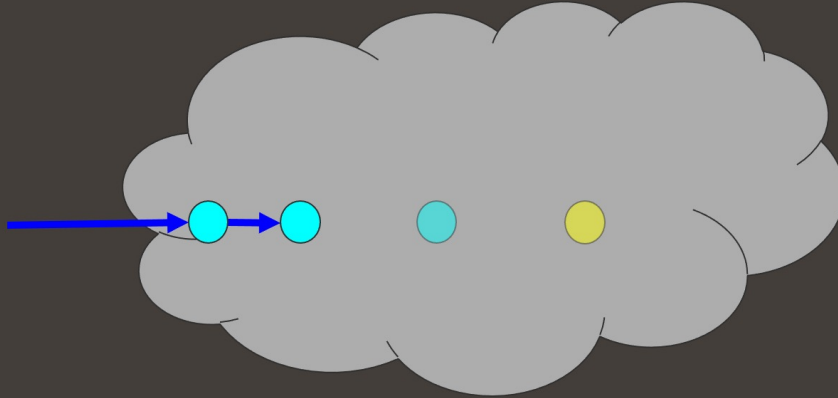


...we have the distance and  $\mu_{bar}$  to compute  $T_{bar}$ , and we know  $P_n$  and  $P_s$  based on the tracking algorithm we use.

## Form a path using Null-Collision Tracking

Incremental distance sampling with  $P_n, P_s$  test:

$$p_{null}(\bar{x}) = \bar{T}(x_0, x_1) \bar{u}(x_1) P_n(x_1) \bar{T}(x_1, x_2) \bar{u}(x_2) P_n(x_2)$$

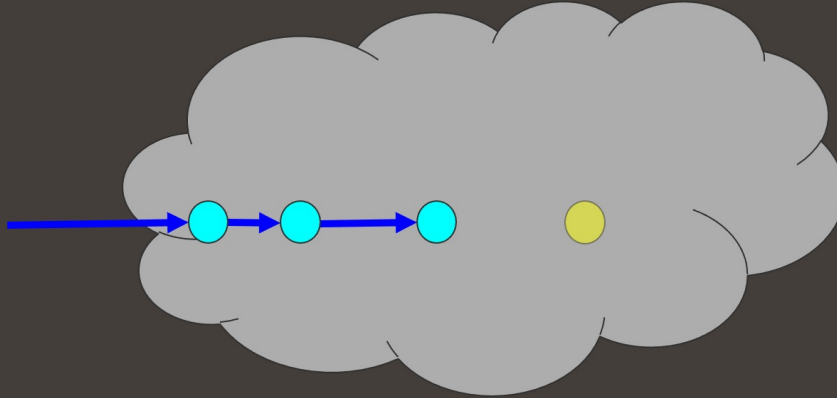


For all the vertices before the scattering, we apply pdf  $P_n$ ...

## Form a path using Null-Collision Tracking

Incremental distance sampling with  $P_n, P_s$  test:

$$p_{null}(\bar{x}) = \bar{T}(x_0, x_1) \bar{u}(x_1) P_n(x_1) \bar{T}(x_1, x_2) \bar{u}(x_2) P_n(x_2) \\ \bar{T}(x_2, x_3) \bar{u}(x_3) P_n(x_3)$$



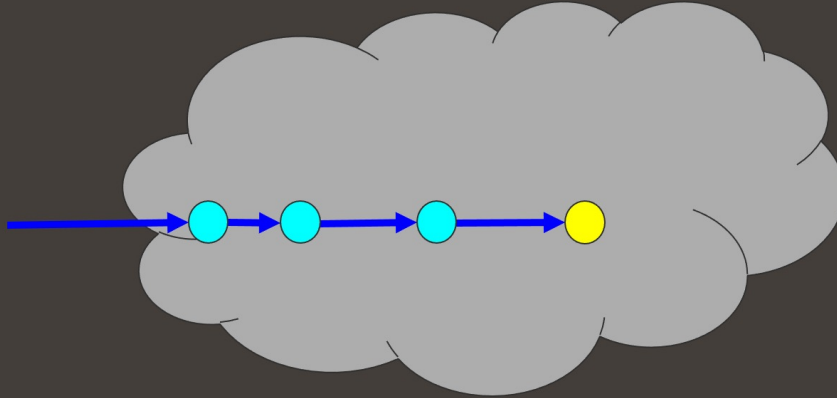
...repeat the distance sampling process and update the corresponding pdf...



## Form a path using Null-Collision Tracking

Incremental distance sampling with  $P_n, P_s$  test:

$$p_{null}(\bar{x}) = \bar{T}(x_0, x_1) \bar{u}(x_1) P_n(x_1) \bar{T}(x_1, x_2) \bar{u}(x_2) P_n(x_2) \\ \bar{T}(x_2, x_3) \bar{u}(x_3) P_n(x_3) \bar{T}(x_3, x_k) \bar{u}(x_k) P_s(x_k)$$



...until we reach the scattering point and apply pdf  $P_s$

## MIS Weight

Lots of terms can be cancelled out to compute MIS weight:

$$f(\bar{x}) = \bar{T}(x_0, x_1)u_n(x_1)\bar{T}(x_1, x_2)u_n(x_2)\dots\bar{T}(x_{k-1}, x_k)u_s(x_k)$$

$$p_{probes}(\bar{x}) = p_{select}(x_k)\bar{T}(x_0, x_1)\bar{u}(x_1)\bar{T}(x_1, x_2)\bar{u}(x_2)\dots\bar{T}(x_{k-1}, x_k)$$

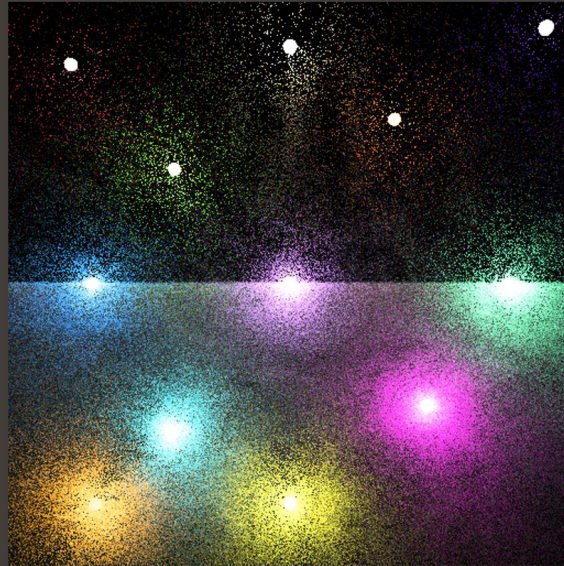
$$p_{null}(\bar{x}) = \bar{T}(x_0, x_1)\bar{u}(x_1)P_n(x_1)\bar{T}(x_1, x_2)\bar{u}(x_2)P_n(x_2)\dots\bar{T}(x_{k-1}, x_k)\bar{u}(x_k)P_s(x_k)$$

$$p_{null}(\bar{x}):p_{probes}(\bar{x}) = P_n(x_1)\dots P_n(x_{k-1})\bar{u}(x_k)P_s(x_k):p_{select}(x_k)$$

The contribution function and the path pdf looks quite verbose, but lots of the terms can actually be cancelled. We can then use the final simplified terms to form the mis weight.

# Null-Collision Tracking

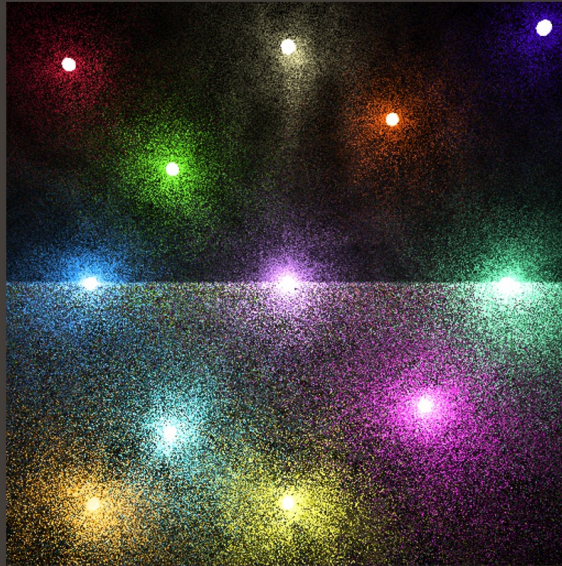
Heterogeneous volume with low (top) and high (down) extinction coefficients



This is a test render of forward-scattering heterogeneous volume with strong lights embedded within. Null-collision tracking doesn't do well on thinner volumes here.

# Probe Spheres

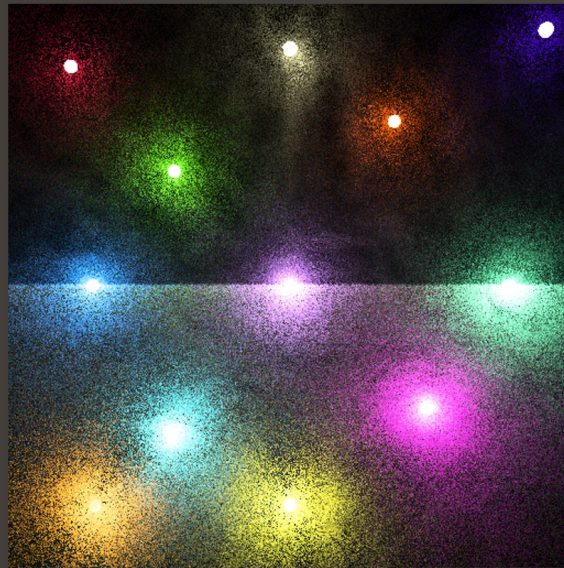
Heterogeneous volume with low (top) and high (down) extinction coefficients



...and this is an equal sample count test render using our probe sphere strategy. it does well in the thin volume but behaves worse in the thicker volume.

# MIS

Heterogeneous volume with low (top) and high (down) extinction coefficients



And this is a test render using MIS to combine the two strategies, and now we have both cases covered in one unified volume integrator.





This is an equal-sample-count production shot test. The upside one is a render using our emission sampling improvements. The downside one is a render where we further layer in our scattering sampling improvements. You can see that the noise is further reduced around the atmospheric area illuminated by the emissive sources.

## Production Results



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SIGGRAPH 2021

And here are some still frames from the film *Raya and the Last Dragon*, showcasing the beautiful work our artists put together using our improved volume integrator.

## Production Results



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The renderer can handle more combinations of complex lighting and volumetric scenarios now...



## Production Results



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We can use emissive volumes to produce more realistic and accurate shadow movements

## Production Results



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SIGGRAPH 2021

...and we can now also render more volumetric effects directly using our renderer

## Production Results



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SIGGRAPH 2021

...which reduces the complexity of our compositing setups

# Production Results





# Production Results



# Production Results



## Production Results



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...and of course we are very happy with our ability to still render white clouds efficiently.

# Conclusion & Future Work

We presented:

- Two sample improvements for low order emission and scattering
- More robust system for common volume scenarios (atmosphere/godray/fire)

Areas for future work:

- Extends our techniques for indirect illumination
- Still lots of spaces for improvement (volume caustics, better volume sampling after surface bounces, occlusion)

To summarize: We improved our volume emission and scattering sampling through extending the null-collision formulation. These improvements make our rendering system more robust handling various common volume scenarios, without losing its strength for high order scattering.

In the future, we would like to have scattering sample technique that is not limited to primary ray direct lighting. Better sampling for volume caustic and complex occlusion without losing the performance would be always desired.



# SIGGRAPH ADDITIONAL DISNEY TALKS SLIDE PLACEHOLDER

Information will be provided closer to the event.  
Will possibly contain 1-3 slides of Disney talk information.



Placeholder slide where we will place information related to other Walt Disney Animation Studios presentations taking place around Siggraph 2021



SIGGRAPH 2021

**THANK YOU**

**FOR JOINING US!**



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THE PREMIER CONFERENCE & EXHIBITION IN  
COMPUTER GRAPHICS & INTERACTIVE TECHNIQUES

We thank you for joining the talk and look forward to discuss with you later. See you in the rest of SIGGRAPH